Quark Matter May Not Be Strange

Bob Holdom,^{*} Jing Ren,[†] and Chen Zhang[‡] Department of Physics, University of Toronto, Toronto, Ontario M5S1A7, Canada

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If quark matter is energetically favored over nuclear matter at zero temperature and pressure, then it has long been expected to take the form of strange quark matter (SQM), with comparable amounts of u, d, and squarks. The possibility of quark matter with only u and d quarks (udQM) is usually dismissed because of the observed stability of ordinary nuclei. However, we find that udQM generally has lower bulk energy per baryon than normal nuclei and SQM. This emerges in a phenomenological model that describes the spectra of the lightest pseudoscalar and scalar meson nonets. Taking into account the finite size effects, udQM can be the ground state of baryonic matter only for baryon number $A > A_{min}$ with $A_{min} \gtrsim 300$. This ensures the stability of ordinary nuclei and points to a new form of stable matter just beyond the periodic table.

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Introduction.—Hadronic matter is usually thought to be the ground state of baryonic matter (matter with a net baryon number) at zero temperature and pressure. Then, quark matter only becomes energetically favorable in an environment like a heavy ion collider or deep inside a neutron star. However, as proposed by Witten [1] (with some relation to earlier work [2–5]), quark matter with comparable numbers of u, d, and s, also called strange quark matter (SQM), might be the ground state of baryonic matter, with an energy per baryon $\varepsilon \equiv E/A$ even smaller than 930 MeV for the most stable nuclei ⁵⁶Fe.

With the lack of a first-principles understanding of the strong dynamics, the MIT bag model [6] has long been used as a simple approximation to describe quark matter. In this model, constituent quark masses vanish inside the bag, and SQM is found to reach lower energy than quark matter with only *u* and *d* quarks (*ud*QM). If SQM is the ground state down to some baryon number A_{\min} , as long as the transition of ordinary heavy nuclei with $A > A_{\min}$ to SQM needs a simultaneous conversion of a sufficiently large number of down quarks to strange quarks, the conversion rate can be negligibly small [7]. A faster catastrophic conversion could occur if the ground state were instead *ud*QM. So, quite often, the energy per baryon is required to satisfy $\varepsilon_{\text{SOM}} \lesssim 930 \text{ MeV} \lesssim \varepsilon_{udOM}$ [7,8].

On the other hand, since the periodic table of elements ends for $A \gtrsim 300$, this catastrophe can be avoided if $A_{\min} \gtrsim 300$ for *ud*QM. It is also recognized that the bag model may not adequately model the feedback of a dense quark gas on the QCD vacuum. How the u, d, and s constituent quark masses respond to the gas should account for the fact that flavor symmetry is badly broken in QCD. This can be realized in a quark-meson model by incorporating in the meson potential the flavor-breaking effects originating in the current quark masses. Through the Yukawa term, the quark densities drive the scalar fields away from their vacuum values. The shape of the potential will then be important to determine the preferred form of quark matter. This effect has already been seen in NJL and quark-meson models [9–13]. These are studies in the bulk limit, and they tend to find that udQM has a lower ε than SQM, with the conclusion that neither is stable.

The possibility that *ud*QM is actually the ground state of baryonic matter has been ignored in the literature, but it shall be our focus in this Letter. With an effective theory for only the scalar and pseudoscalar nonets of the sub-GeV mesons with Yukawa coupling to quarks, we demonstrate a robust connection between the QCD spectrum and the conditions for a *ud*QM ground state in the bulk, i.e., $\varepsilon_{udQM} \lesssim 930$ MeV and $\varepsilon_{udQM} < \varepsilon_{SQM}$. We shall also show that surface effects are of a size that can ensure that $A_{min} \gtrsim$ 300 by numerically solving the scalar field equation of motion. This points to the intriguing possibility that a new form of stable matter consisting only of *u* and *d* quarks might exist not far beyond the end of the periodic table.

The meson model.—Here we study an effective theory describing the mass spectra and some decay rates of the scalar and pseudoscalar nonets of the sub-GeV mesons. The QCD degrees of freedom not represented by these mesons are assumed to be integrated out and encoded in the parameters of the phenomenological meson potential. We view our description as dual to one that contains vector mesons [14]. With the parameters determined from data, we can then extrapolate from the vacuum field values to the smaller field values of interest for quark matter.

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We find that a linear sigma model provides an adequate description without higher-dimensional terms:

$$\mathcal{L}_m = \mathrm{Tr}(\partial_\mu \Phi^{\dagger} \partial^\mu \Phi) - V, \qquad V = V_{\mathrm{inv}} + V_b, \quad (1)$$

where $\Phi = T_a(\sigma_a + i\pi_a)$ is the meson field and $T_a = \lambda_a/2$ (a = 0, ..., 8) denotes the nine generators of the flavor U(3) with $\text{Tr}(T_aT_b) = \delta_{ab}/2$. V_{inv} is chirally invariant:

$$V_{\rm inv} = \lambda_1 ({\rm Tr} \Phi^{\dagger} \Phi)^2 + \lambda_2 {\rm Tr}[(\Phi^{\dagger} \Phi)^2] + m^2 {\rm Tr}(\Phi^{\dagger} \Phi) - c(\det \Phi + {\rm H.c.}).$$
(2)

The *c* term is generated by the 't Hooft operator. Boundedness from below requires that $\lambda_1 + \lambda_2/2 > 0$. For there to be spontaneous symmetry breaking in the absence of V_b requires that $8m^2(3\lambda_1 + \lambda_2) < c^2$.

 $V_b = \sum_{i=1}^{8} V_{bi}$ describes the explicit SU(3) flavor breaking by incorporating the current quark mass matrix $\mathcal{M} = \text{diag}(m_{u0}, m_{d0}, m_{s0})$:

$$V_{b1} = b_{1} \operatorname{Tr}(\Phi^{\dagger} \mathcal{M} + \operatorname{H.c.}),$$

$$V_{b2} = b_{2} \epsilon_{ijk} \epsilon_{mnl} \mathcal{M}_{im} \Phi_{jn} \Phi_{kl} + \operatorname{H.c.},$$

$$V_{b3} = b_{3} \operatorname{Tr}(\Phi^{\dagger} \Phi \Phi^{\dagger} \mathcal{M}) + \operatorname{H.c.},$$

$$V_{b4} = b_{4} \operatorname{Tr}(\Phi^{\dagger} \Phi) \operatorname{Tr}(\Phi^{\dagger} \mathcal{M}) + \operatorname{H.c.},$$

$$V_{b5} = b_{5} \operatorname{Tr}(\Phi^{\dagger} \mathcal{M} \Phi^{\dagger} \mathcal{M}) + \operatorname{H.c.},$$

$$V_{b6} = b_{6} \operatorname{Tr}(\Phi \Phi^{\dagger} \mathcal{M} \mathcal{M}^{\dagger} + \Phi^{\dagger} \Phi \mathcal{M}^{\dagger} \mathcal{M}),$$

$$V_{b7} = b_{7} (\operatorname{Tr} \Phi^{\dagger} \mathcal{M} + \operatorname{H.c.})^{2},$$

$$V_{b8} = b_{8} (\operatorname{Tr} \Phi^{\dagger} \mathcal{M} - \operatorname{H.c.})^{2}.$$
(3)

Other possible terms have been eliminated by a field redefinition [15]. We adopt $m_{s0} = 94$ MeV and $m_{u0,d0} = m_{ud0} = 3.4$ MeV [16]. This general set of terms is successful at describing the lightest scalar and pseudoscalar nonets, with all masses below 1 GeV, which is typically not possible when keeping the V_{b1} term only [17–19]. The sizes of the b_i coefficients are made more meaningful by normalizing with respect to the estimates of naive dimensional analysis (NDA) [20] to obtain dimensionless NDA couplings:

$$\bar{\lambda}_{1,2} = \frac{f_{\pi}^2}{\Lambda^2} \lambda_{1,2}, \qquad \bar{m}^2 = \frac{1}{\Lambda^2} m^2, \qquad \bar{c} = \frac{f_{\pi}}{\Lambda^2} c, \\
\bar{b}_1 = \frac{1}{f_{\pi}\Lambda} b_1, \qquad \bar{b}_2 = \frac{1}{\Lambda} b_2, \qquad \bar{b}_{3,4} = \frac{f_{\pi}}{\Lambda} b_{3,4}, \\
\bar{b}_{5-8} = b_{5-8}, \qquad (4)$$

where f_{π} is the pion decay constant and $\Lambda = 4\pi f_{\pi}$ is an effective cutoff.

In the meson model, chiral symmetry breaking of QCD is realized by the nonzero vacuum expectation values of the neutral scalar meson fields at the potential minimum,

 $\langle \Phi \rangle = T_0 v_0 + T_8 v_8 = \frac{1}{2} \operatorname{diag}(v_n, v_n, \sqrt{2}v_s)$, where we use the nonstrange and strange flavor basis: $\sigma_n = (\sqrt{2}/\sqrt{3})\sigma_0 + (1/\sqrt{3})\sigma_8$, $\sigma_s = (1/\sqrt{3})\sigma_0 - (\sqrt{2}/\sqrt{3})\sigma_8$. The deformation by \mathcal{M} naturally implies an SU(3) breaking vacuum $v_n \neq \sqrt{2}v_s$. A standard gauging of the model then leads to $v_n = f_\pi = 92$ MeV, $v_s = \sqrt{2}f_K - f_\pi/\sqrt{2} = 90.5$ MeV [16,18].

The mass spectra for the scalar and pseudoscalar nonets are derived by $\mathbb{M}_{s,ab}^2 = \partial^2 V / \partial \sigma_a \partial \sigma_b$ and $\mathbb{M}_{p,ab}^2 = \partial^2 V / \partial \pi_a \partial \pi_b$. With isospin symmetry, the eight independent masses are $m_{a_0}^2 = \mathbb{M}_{s,11}^2$, $m_{\kappa}^2 = \mathbb{M}_{s,44}^2$, $m_{\pi}^2 = \mathbb{M}_{p,11}^2$, $m_K^2 = \mathbb{M}_{p,44}^2$, and m_{σ}^2 , $m_{f_0}^2$, m_{η}^2 , $m_{\eta'}^2$ after diagonalizing the (0,8) sectors. The rotations are defined as $\sigma_0 = \cos \theta_s \sigma - \sin \theta_s f_0$, $\sigma_8 = \sin \theta_s \sigma + \cos \theta_s f_0$, and $\pi_0 = \cos \theta_p \eta' - \sin \theta_p \eta$, $\pi_8 = \sin \theta_p \eta' + \cos \theta_p \eta$.

We solve the 12 free parameters $(\lambda_1, \lambda_2, c, m^2, b_1, ..., b_8)$ in Eq. (1) in terms of two decay constants, eight meson masses, and two mixing angles. θ_p is related to the diphoton radiative decay widths of η' , η and the strong decay widths of a_0 , κ . θ_s needs to fit the small and large $\pi\pi$ widths of f_0 and σ , respectively, which implies that the σ meson is quite close to the nonstrange direction.

Table I presents two benchmarks for the meson model. The parameters of set 1 are chosen to give a good fit to the data; however, this leads to a rather large value for the NDA coupling \bar{b}_6 . Given the theoretical uncertainties associated with the neglected higher-dimensional terms, allowing the masses and decay widths to depart from the experimental values could be more sensible. An example with up to 10% departures gives the smaller NDA couplings of set 2.

Table II compares the experimental values [16] with the results of the two benchmarks, including predictions for some decay widths. The f_0 , a_0 widths have large KK threshold corrections, and so for these, Flatté [21] rather than Breit-Wigner widths are used. In these cases, we also compare the ratios R_{f_0} , R_{a_0} that involve the strange and nonstrange amplitudes [22,23]. We have checked that turning on explicit isospin breaking ($m_{u0} \neq m_{d0}$) has negligible impact on this study. But it does turn on the $\pi^0 - \eta(\eta')$ mixing angles, ϵ and ϵ' . ϵ is found to be roughly consistent with experiments.

Quark matter in general.—Now we can employ the meson model to study quark matter. Quark matter can

TABLE I. The NDA couplings for benchmarks.

	$\bar{\lambda}_1$	$\bar{\lambda}_2$	\bar{m}^2	ī	\bar{b}_1	\bar{b}_2
Set 1 Set 2	-0.06 0.04	0.33 0.16	-0.13 0.05	0.33 0.27	-4.4 -1.6	0.19 -0.14
Set 1 Set 2	\bar{b}_3 -4.2 -0.18	$ar{b}_4 \\ 2.5 \\ 0.09$	$ar{b}_5 \\ -3.0 \\ 4.0$	$ar{b}_6$ 50 5.2	$ar{b}_7$ 1.4 -3.9	$ar{b}_8 \\ 4.7 \\ -5.5$

	m_{π}	m_K	m_{η}	m'_η	θ_p
Exp.	138	496	548	958	
Set 1	138	496	548	958	-15.0°
Set 2	148	454	569	922	-10.8°
	m_{a_0}	m_{κ}	m_{σ}	m_{f_0}	θ_s
Exp.	980 ± 20	700–900	400-550	990 ± 20	
Set 1	980	900	555	990	31.5°
Set 2	887	916	555	955	21.7°
	$\Gamma_{n \to \gamma \gamma}$	$\Gamma_{n' \to \gamma \gamma}$	$\Gamma_{\sigma \to \pi\pi}$	$\Gamma_{\kappa \to K\pi}$	
Exp.	0.52-0.54	4.2-4.5	400-700	~500	
Set 1	0.59	4.90	442	451	
Set 2	0.54	4.87	422	537	
	$\Gamma_{f_0 \to \pi\pi}$	R_{f_0}	$\Gamma_{a_0 \to n\pi}$	R_{a_0}	
Exp.	10-100	3.8-4.7	50-100	1.2-1.6	
Set 1	11	4.3	37.4	2.4	
Set 2	20	4.0	52.0	1.2	

TABLE II. The meson masses (in MeV), mixing angles, and decay widths (in MeV, keV for scalar, pseudoscalar).

become energetically favorable due to the reduction of the constituent quark masses in the presence of the quark densities. QCD confinement, on the other hand, prevents net color charge from appearing over large volumes. We suppose that these residual QCD effects on the energy per baryon are minor, similar to the way they are minor for the constituent quark model description of much of the QCD spectrum.

With the Yukawa coupling to quarks, $\mathcal{L}_y = -2g\bar{\psi}\Phi\psi$, the equations of motion for the spherically symmetric meson fields of interest are [26,27]

$$\nabla^{2}\sigma_{n}(r) = \frac{\partial V}{\partial\sigma_{n}} + g \sum_{i=u,d} \langle \bar{\psi}_{i}\psi_{i} \rangle,$$

$$\nabla^{2}\sigma_{s}(r) = \frac{\partial V}{\partial\sigma_{s}} + \sqrt{2}g \langle \bar{\psi}_{s}\psi_{s} \rangle,$$
 (5)

where $\nabla^2 = (d^2/dr^2) + (2/r)(d/dr)$, and there are $N_C = 3$ colors of quarks. The quark gas is described by the Fermi momentum for each flavor, $p_{Fi} = p_F f_i^{1/3}$, where the quark fractions are $f_i = n_i/(N_C n_A)$, $p_F = (3\pi^2 n_A)^{1/3}$ and n_A is the baryon number density. The *r* dependence of these quantities is determined by the equations of hydrostatic equilibrium.

The forces driving the field values are from the scalar potential and the quark gas densities, $\langle \bar{\psi}_i \psi_i \rangle = [2N_C/(2\pi)^3] \int_0^{p_{Fi}} d^3 p m_i / \sqrt{p^2 + m_i^2}$. In the interior, the quark masses $m_{u,d}(r) = g\sigma_n(r) + m_{ud0}$ and $m_s(r) = \sqrt{2}g\sigma_s(r) + m_{s0}$ become smaller than the vacuum values m_{udv} and m_{sv} . The radius *R* of the bound state is defined where $\sigma_i(r)$ and $p_{Fi}(r)$ quickly approach their vacuum values.

Electrons have little effect on the energy per baryon for any A, and they need not be contained when R becomes smaller than the electron Compton wavelength, i.e., $A \lesssim 10^7$ [7]. The quark, scalar, and Coulomb energy densities are [7,28]

$$\rho_{\psi} = \sum_{i=u,d,s} \frac{2N_C}{(2\pi)^3} \int_0^{p_{Fi}} d^3 p \sqrt{p^2 + m_i^2},
\rho_{\phi} = \Delta V + \frac{1}{2} \sum_{i=n,s} (\nabla \sigma_i)^2, \qquad \rho_Z = \frac{1}{2} \sqrt{\alpha} V_C n_Z, \quad (6)$$

where ΔV is the potential energy with respect to the vacuum. $n_Z = \frac{2}{3}n_u - \frac{1}{3}(n_d + n_s)$ is the charge density, V_C is the electrostatic potential, and $\alpha = 1/137$. The flavor composition of the quark gas and the radius *R* can be determined by minimizing the energy of the bound state $E = \int_0^R d^3 r (\rho_{\psi} + \rho_{\phi} + \rho_Z)$ [29].

Quark matter in the bulk limit.—At large A, finite size effects can be ignored, and then both the meson fields and quark densities can be taken to be spatially constant. From Eq. (5) and for given (p_F, f_i) , the meson fields take values where the two forces balance. Among these forcebalancing points we can find the values of (\bar{p}_F, \bar{f}_i) that minimize the energy per baryon $\varepsilon = (\rho_{\psi} + \rho_{\phi} + \rho_Z)/n_A$, with the uniform charge density $\rho_Z = (4\pi/5)\alpha R^2 n_Z^2$. The flavor composition \bar{f}_i is driven to charge neutrality in the large-A limit to avoid the dominance of ρ_Z .

Figure 1 presents the field values and the energy per baryon as functions of p_F , after minimization with respect to f_i , for the set 1 benchmark with $m_{udv} = 330$ MeV (which implies g = 3.55 and $m_{sv} = 548$ MeV). The minimum energy per baryon is $\bar{\epsilon} = 903.6$ (905.6) MeV at $\bar{p}_F =$ 367.8 (368.5) MeV with $\bar{f}_s \approx 0$ for set 1 (set 2). For both sets, udQM is the ground state of baryonic matter in the bulk.

As p_F increases from small values, the fields move away from the vacuum along the least steep direction, which is a valley oriented close to the σ_n direction. σ_n drops rapidly at $p_F^{(n)}$, and at \bar{p}_F the minimal energy per baryon $\bar{\epsilon}$ is reached. \bar{p}_F can be estimated by minimizing the relativistic quark



FIG. 1. The field values σ_n , σ_s (blue dashed, left axis) and the energy per baryon number ε (red solid, right axis) in the bulk limit. The vertical lines denote the values of $p_F^{(n)}$, \bar{p}_F , and $p_F^{(s)}$.



FIG. 2. The bulk limit $\bar{\varepsilon}$ vs m_{σ} from the parameter scan.

and potential energies $\varepsilon \approx \frac{3}{4}N_C p_F \chi + 3\pi^2 \Delta V_n / p_F^3$ with respect to p_F only. $\chi = \sum_i f_i^{4/3}$, and ΔV_n is the potential difference along the valley. This gives $\bar{\varepsilon} \approx N_C \bar{\chi} \bar{p}_F$ and $\bar{p}_F^4 \approx 12\pi^2 \Delta V_n / (N_C \bar{\chi})$, with only *u* and *d* quarks contributing in $\bar{\chi}$. f_s will finally turn on for $p_F \gtrsim p_F^{(s)}$ when it is energetically favorable to produce strange quarks (that may or may not be relativistic).

Our conclusion regarding *ud*QM relies on the features that $p_F^{(n)} \leq \bar{p}_F \leq p_F^{(s)}$ and $\bar{\epsilon} \leq 930$ MeV. These quantities can be estimated with a parameter scan of the meson model along with $m_{udv} \approx 330-360$ MeV. The scan is constrained to be no more than about 10% outside the experimental ranges and with NDA coupling magnitudes less than 15. We find the ranges $p_F^{(n)} \approx 280-305$ MeV, $\bar{p}_F \approx 355-$ 395 MeV, $p_F^{(s)} \gtrsim 550$ MeV, and $\bar{\epsilon} \approx 875-960$ MeV. As an example of sensitivity to the lightest meson masses, Fig. 2 shows a $\bar{\epsilon}$ vs m_{σ} projection of the parameter space, where we see that realistic values of m_{σ} favor stable *ud*QM.

Determination of A_{\min} for udQM.—At smaller A, we need to include finite size effects and the Coulomb energy contribution. We adopt the approximation that the values of p_F and f_i are constants, nonvanishing only for r < R, which has been found to give a good approximation for the binding energy [30]. For each A, we solve for the profile of the field $\sigma_n(r)$ moving along the valley using Eq. (5) and find the configuration, including the radius R, that minimizes the energy E.

For the set 1 benchmark with $m_{udv} = 330$ MeV, the numerical solutions of the electric charge and the minimal energy per baryon as functions of A are presented by blue dots in Figs. 3 and 4, respectively. It turns out that the electric charge of udQM can be well estimated by simply minimizing the quark and Coulomb energies of the relativistic u, dgas with charge $Z = N_C A [\bar{f}_u(A) - 1/3]$, as shown by the blue line in Fig. 3. We find $Z \approx (0.86/\alpha N_C) A^{1/3}$ for large A. The shaded region denotes configurations that are stable against decays into ordinary nuclei.

Figure 4 shows that the surface effect increases the energy and destabilizes the udQM configuration for



FIG. 3. The electric charge of *ud*QM: full result (blue dots) and the bulk approximation (blue line).

 $A < A_{\min}$. For set 1 (set 2), $A_{\min} \approx 320$ (450) is large enough to prevent normal nuclei from decaying to udQM. The numerical results of $\bar{e}(A)$ can be well approximated by incorporating a surface-tension term $4\pi R^2 \Sigma$ into the bulk analysis: $\bar{e}(A) \approx \bar{e} + 46\Sigma/(\bar{p}_F^2 A^{1/3}) + 0.31\alpha Z^2 \bar{p}_F/A^{4/3}$. Here \bar{e} and \bar{p}_F reflect the value of $\bar{\chi}$ away from the bulk limit. From fits from the two sets and other examples, we find that $\Sigma \approx (91 \text{ MeV})^3$, and that it varies less than \bar{e} as displayed in Fig. 2. So as long as $\bar{e} \gtrsim 903$ MeV, we can expect that $A_{\min} \gtrsim 300$. The surface term dominates the Coulomb term for all A, and so the analog of fission that ends the periodic table does not occur for udQM.

Discussion.—If A_{min} for udQM is close to the lower limit, it raises the hope to produce this new form of stable matter by the fusion of heavy elements. With no strangeness to produce, this may be an easier task than producing SQM. Due to the shape of the curve in Fig. 3, there would still be the issue of supplying sufficient neutrons in the reaction to produce udQM, as in the attempts to produce normal superheavy nuclei in the hypothetical "island of stability" around $A \approx 300$ [31]. udQM may instead provide a new "continent of stability" as shown in Fig. 3, in which the largest values of Z/A are of interest for production and subsequent decay to the most stable configuration. As with SQM, the further injection of neutrons (or heavy ions



FIG. 4. The minimal energy per baryon $\bar{\epsilon}(A)$ for *udQM* (lower), compared to the charge-neutral configuration (upper).

[32,33]) can cause the piece of *ud*QM to grow with the release of an indefinite amount of energy [34].

Neutron stars could possibly convert to *ud* quark stars. Due to the potential barrier generated by the surface effects, the limiting process for the conversion of a neutron star is the nucleation of a bubble of quark matter initially having the same local flavor composition as the neutron star, via a quantum or thermal tunneling process [35]. There is then a subsequent weak decay to the stable state, SQM or *udQM*, as the bubble grows. The barrier for conversion leads to the possibility that there can coexist both neutron stars and quark stars [36]. In comparison to SQM, udQM predicts a smaller $\bar{\rho} = 4\Delta V_n$ given the same $\bar{\epsilon}$. So *ud* quark stars allow a larger maximum mass, which is of interest for pulsars with $M \sim 2M_{\odot}$ [37,38]. The possible superconducting nature of quark matter in stars may have interesting implications, more so for its transport rather than bulk properties [39].

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^{*}bob.holdom@utoronto.ca

[†]jren@physics.utoronto.ca

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[‡]czhang@physics.utoronto.ca

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